X-ray Structure Refinements and Strain Analysis of Substituted Cubic Lead Pyrochlores $Pb_2(M_{2-y}Pb_y)O_{7-\delta}(0.0 < y < 0.8; M = Nb or Ta)$

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The phase diagrams in the PbO-Nb₂O₅ system and the PbO-Ta₂O₅ system depict pyrochlore structure at certain molar ratios. Compositions Pb₂Nb_{1.51}Pb_{0.49}O_{6.30} (1), Pb₂Ta_{1.4}Pb_{0.6}O_{6.21} (2), and Pb₂Ta_{1.25}Pb_{0.75}O_{6.57} (3) belonging to this family, are refined in the cubic space group $Fd\bar{3}m$ (Z = 8; lattice parameter a = 10.762(1), 10.744(1), 10.757(5) Å, respectively) using the Rietveld refinement approach. The analyses suggest that the B-site is partially occupied by Pb leading to the general formula Pb₂(M_{2-y} Pb_y)O_{7- δ}(0.0 < y < 0.8; M = Nb or Ta). There is an overall broadening observed in the X-ray peak widths in 1, 2, and 3 compared to the Pb-deficient parent phases. It is observed that the X-ray peak widths of 2 is broad, while 3 displays narrow peak widths. It is found via strain analysis that the line broadening observed correlates with the strain in the lattice. © 2001 Academic Press

Key Words: pyrochlore; Rietveld refinement; strain analysis; lead niobates; lead tantalates.

I. INTRODUCTION

Studies of the PbO-Nb₂O₅ and the PbO-Ta₂O₅ systems have indicated the existence of a number of phases with structures apparently related to that of pyrochlore. The pyrochlore structure with the general formula $A_2B_2O_6O'$ is formed by a variety of ions and tolerates a high degree of nonstoichiometry on the O' and the A cation sites (1). It is composed of a network of corner-sharing $(BO_6)_n$ polyhedra, with A cations filling the interstices. The structure consists of two types of cation coordinate polyhedra. The ideal pyrochlore structure crystallizes in the space group $Fd\overline{3}m$ (No. 227) with eight formula units per cell. The origin of the structure can be selected at the A, B, or the O site (1). Typically for lead niobates and tantalates, the assignment is that the A cations occupy the 16(d) site and are 8-coordinated with six equally spaced O anions and two additional axial O' anions, while the smaller B cations

occupy the 16(c) site and are 6-coordinated with all six anions at equal distances from the central cation. The oxygen anions O and O' occupy the $48(f)(x, \frac{1}{8}, \frac{1}{8})$ and 8(b) $(\frac{3}{8}, \frac{3}{8}, \frac{3}{8})$ sites, respectively. Thus a complete description of the three-dimensional arrangement of ions can be derived by the determination and refinement of only one positional parameter x of the O anion at 48(f) site (2). There are four lead niobate pyrochlore phases reported so far with stoichiometries, Pb_{1.5}Nb₂O_{6.5}, Pb₂Nb₂O₇, Pb_{2.5}Nb₂O_{7.5}, and Pb₃Nb₂O₈, all of which display varying degrees of nonstoichiometries at the A-site (3-7). However, among the lead tantalate pyrochlore phases $(Pb_{1.5}Ta_2O_{6.5},$ $Pb_{2.31}Ta_2O_{7.31}$, and $Pb_{2.44}Ta_2O_{7.44}$) the ideal composition Pb₂Ta₂O₇ is unstable but consists of an intergrowth between a Pb-deficient Pb_{1.5}Ta₂O_{6.5} and a Pb-rich $Pb_{22}Ta_{18}O_{67}$ phase (8, 9). It is of interest to note that in all the above compositions the excess Pb is always found to be associated with the A-site. Recently, Sridhar et al. have synthesized solid solutions having a stoichiometry in the range 1.5PbO· M_2O_5 to ~3 PbO· M_2O_5 (M = Nb or Ta) at low temperatures ($\sim 500-600^{\circ}$ C) (10, 11). It was suggested that the excess lead might be at the B-site based on the broadening observed in the preliminary X-ray diffraction patterns. In order to explore the occupancy at the B-site explicitly, we have carried out detailed profile refinements using high-resolution powder X-ray diffraction data. To probe into the cause of the line broadening, the diffraction patterns have been subjected to strain analyses.

In the generally adopted theories (12), two types of structural line broadening are recognized to occur simultaneously: (i) particle-size broadening, caused by finite size of regions in the specimens diffraction incoherently with respect to each other and (ii) strain broadening due to varying displacements of the atom with respect to their reference positions. Normally particle-size broadening is negligibly small and hence ignored. The order dependence of the shape and width of line profiles is studied as a function of these model parameters.

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TABLE 1
Results of EDAX Analyses for $Pb_2(M_{2-v}Pb_v)O_{7-\delta}(0.0 \le y \le 0.8;$
M = Nb, Ta)

	Relative concentration of M ; $M = Nb$, Ta (at. %)			
у	Initial mixtures (Pb:M)	Powder samples (Pb:M)		
0.49	60:40	64:36		
0.60	60:40	64:36		
0.75	69.31	71:29		

II. EXPERIMENTAL

The compounds studied here were synthesized and supplied by Dr. Sreedhar (NCL, Pune, India). A detailed discussion on the low-temperature synthesis ($\sim 500-600^{\circ}$) of these are already described elsewhere (10, 11). Quantitative elemental analyses on all samples were carried out on a JEOL JSM-840 EDAX using Oxford instrument for X-ray analysis software in order to confirm the composition of the metal ions.

High-resolution X-ray diffraction data on Pb₂Nb_{1.51} Pb_{0.49}O_{6.30} (1), Pb₂Ta_{1.4}Pb_{0.6}O_{6.21} (2), and Pb₂Ta_{1.25} Pb_{0.75}O_{6.57} (3) were collected on a STOE/STADI-P X-ray powder diffractometer with germanium monochromated CuK α_1 ($\lambda = 1.54056$ Å) radiation from a sealed tube X-ray generator (20 kV, 25 mA) in the transmission geometry. The samples were rotated during data collection to minimize preferred orientation effect, if any. The data were recorded on a linear PSD. The X-ray data were measured in the range $2\theta = 3$ to 78.60° in steps of 0.02° with 6 s exposure time per step at room temperature.

III. RESULTS AND DISCUSSION

Table 1 gives the results from the EDAX measurements, indicating that the ratio of the metal ions calculated nearly correspond to that of the ions taken initially for syntheses.

a. Profile Refinements

The trial and error indexing program TREOR (13) was used to index all the X-ray patterns. The compounds belong to the cubic system, space group $Fd\overline{3}m$, No. 227. The positional coordinates for the starting model for Rietveld refinements were taken from the published results on the pyrochlore $Pb_{1,5}Ta_2O_{6,5}$ (7). The GSAS (14) package is employed in all the calculations. The profiles were fitted using a pseudo-Voigt function that has three Gaussian and two Lorenztian coefficients. A cosine-Fourier function consisting of three to seven coefficients was used to define the background. The coordinate of the oxygen atom in the 48(f) position was first refined to convergence (All heavy atoms are in special positions in this space group), holding the occupancy and the thermal parameters fixed. Then the occupancies of Pb and M (Nb or Ta) were refined keeping the overall occupancy for the site fixed. Isotropic thermal parameters were then refined alternately with the occupancies. Since the refinements remained stable even after the oxygen occupancies were allowed to refine and the values obtained were in agreement with the limits of the expected values, it was discerned to accept the refined occupancy values. However, a detailed neutron diffraction study would ascertain the oxygen occupancy values with a higher degree of confidence. Details of the crystal data and refinements are given in Table 2.

Crystal Data for $10_2(M_{2-y}, 10_y)O_{7-\delta}$, $(0 < y < 0.8)$, $M = 140$ of Ta				
Formula	$Pb_2Nb_{1.51}Pb_{0.49}O_{6.30}$	$Pb_{2}Ta_{1.4}Pb_{0.6}O_{6.21}$	$Pb_2Ta_{1.25}Pb_{0.75}O_{6.57}$	
Formula weight	768.184	899.816	903.227	
Color	Yellow	Yellow	Yellow	
Space group	$Fd\overline{3}m$	$Fd\overline{3}m$	$Fd\overline{3}m$	
Ζ	8	8	8	
$\lambda(\text{\AA})$	1.54056	1.54056	1.54056	
2θ	3°-78.60°	3°-78.60°	3°-78.60°	
No. of reflections	30	29	29	
No. of structural parameter	10	10	10	
a (Å)	10.762(1)	10.744(1)	10.757(2)	
$V(Å^3)$	1246.46(20)	1240.22(20)	1244.73(30)	
$R_{\rm wp}$ (%)	11.84	10.60	9.98	
$R_{\rm p}(\%)$	9.02	8.25	7.46	
R(I, hkl) (%)	3.91	4.31	4.54	
No. of data points	3781	3781	3781	

TABLE 2 Crystal Data for $Pb_{2}(M_{2-y}Pb_{y})O_{7-s}$; (0 < y < 0.8), M = Nb or Ta



FIG. 1. Observed, calculated, and difference X-ray diffraction pattern of (1).

The structure reports on the lead antimonate pyrochlore Pb₂ (Sb_{2-x}Pb_x)O_{7- δ} and lead ruthenate pyrochlore Pb₂ (Ru_{2-x}Pb_x)O_{7- δ} (15, 16) suggest the presence of Pb⁴⁺ in the B-site. The lattice parameters *a*, for these two cases are 10.66 and 10.58 Å, respectively. These values are less than the *a* parameter values found in **1**, **2**, and **3**. It may be argued that this small difference in the lattice parameter is due to the differences in the ionic radii of the M^{5+} (Nb or Ta) and Sb⁵⁺ cations (17). Hence, it may be conjectured that the oxidation state of Pb in the B-site is 4+.

The observed, difference, and calculated patterns of all the three phases are shown in Figs. 1, 2, and 3. Tables 3a–3c list the final positional coordinates along with isotropic thermal parameters and Table 3d lists the bond lengths for all the phases. Figure 4 shows the octahedral coordination at the B site.

The Rietveld refinement results suggest the formation of a cubic pyrochlore solid solution with partial occupancy of Pb in the B-site leading to the formula Pb₂ $(M_{2-y}Pb_y)$ $O_{7-\delta}(0.0 < y < 0.8; M = Nb \text{ or Ta})$. It is observed from the X-ray patterns that there is a significant broadening of the



FIG. 2. Observed, calculated, and difference X-ray diffraction pattern of (2).

peaks in 2 compared to that seen in 3 and the parent compound (Fig. 5).

Sreedhar *et al.* (10) have observed that a cubic solid solution with part of the Pb in the B-site was formed in Nb pyrochlores for the sample with a PbO/Nb₂O₅ molar ratio of 2. Also it was observed that a minor amount of unreacted PbO was present when the PbO/Nb₂O₅ molar ratio was raised 3.5, suggesting that the maximum ratio is limited to 3.5. In case of the PbO-Ta₂O₅ system, the diffraction lines show significant broadening for the molar ratio ≤ 2.0 , while for the higher molar ratios (>2.3), the peak widths are narrowed. At this stage, a strain analysis was undertaken to evaluate these features.

b. Strain Analysis

A generally applicable one-dimensional model based on the distortion of the lattice (18, 19) has been used to obtain the average microstructural parameters like crystal size and strain along different directions of the lattice employing individual (hkl) reflections. The corrected experimental



FIG. 3. Observed, calculated, and difference X-ray diffraction pattern of (3).

X-ray profile that was used for Rietveld analysis was matched with the simulated profile using the equations

$$I(s) = I_{N-1}(s) + I'_N(s),$$

where $I'_N(s)$ is the modified intensity for the probability peak centered at D (= Nd_{hkl}). It has been shown that

$$I'_{N}(s) = (2 a_{N}/D\pi^{1/2}) \exp(idNs) [1 - a_{N}s \{2D(a_{N}s) + i\pi^{1/2} \exp(-a_{N}^{2}s^{2})\}],$$

where $a_N^2 = Nw^2$ and $D(a_N s)$ is the Dawson's integral or the error function with purely complex argument and can be easily computed. N is the number of unit cells counted in a direction perpendicular to the (*hkl*) Bragg plane. The experimental profile between s_o and $s_0 + s_o/2$ (or s_o and $s_o + B/2d$, if there is truncation of the profile B < 1) is matched with the corresponding simulated order of reflection between s_o and $s_o/2$ (or s_o and $s_o + B/2d$) using a onedimensional distorted model for various values of N and

TABLE 3

Atom	Site	x	у	Ζ	0	$U_{\rm iso}({\rm \AA}^2)$	
(a) Final atomic coordinates from powder X-ray data at							
$\mathbf{D}\mathbf{L}(1)$	1(())	298 K 101	PD ₂ ND	$1.51Pb_{0.49}$	$O_{6.30}$	0.0225(10)	
PD(1)	10(d)	0.5	0.5	0.5	1.000(5)	0.0333(10)	
ND(1)	16(C)	0.0	0.0	0.0	0.753(6)	0.01287(11)	
Pb(2)	16(c)	0.0	0.0	0.0	0.2426(6)	0.01287(11)	
O(1)	48(f)	0.3171(11)	0.125	0.125	1.000	0.04711(5)	
O(2)	8(b)	0.375	0.375	0.375	0.305(51)	0.04711(5)	
	(b) Fina	l atomic cooi	dinates	from pow	der X-ray da	ata at	
		298 K for	r Pb ₂ Ta ₁	$_{1.40}Pb_{0.60}$	O _{6.21}		
Pb(1)	16(d)	0.5000	0.5	0.5	1.000(3)	0.0224(1)	
Ta(1)	16(c)	0.0000	0.0	0.0	0.702(81)	0.0217(1)	
Pb(2)	16(c)	0.0000	0.0	0.0	0.299(81)	0.0217(1)	
O(1)	48(f)	0.3356(7)	0.125	0.125	1.000	0.0285(5)	
O(2)	8(b)	0.375	0.375	0.375	0.210(10)	0.0285(5)	
	(c) Fina	l atomic cooi	dinates	from pow	der X-ray da	ata at	
		298 K for	r Pb ₂ Ta ₁	$1.25 Pb_{0.75}$	O _{6.57}		
Pb(1)	16(d)	0.5000	0.5	0.5	1.000(1)	0.0179(9)	
Ta(1)	16(c)	0.0000	0.0	0.0	0.625(2)	0.0168(1)	
Pb(2)	16(c)	0.0000	0.0	0.0	0.375(2)	0.0168(1)	
O(1)	48(f)	0.3206(15)	0.125	0.125	1.000	0.0524(3)	
O(2)	8(b)	0.375	0.375	0.375	0.448(10)	0.0524(3)	
,	0						
(d) Bond distances (A) in $Pb_2(M_{2-y}Pb_y)O_{7-\delta}$ (0.0 < y < 0.8);							
Dand di	atomaa (Å)	Dh Nih Dh	M = IND	OF LA DE TO DI		To Dh O	
Bond di	stance (A)	P0 ₂ N0 _{1.51} P0 ₀	0.49U _{6.30}	$PO_2 Ia_{1.4}PC$	$D_{0.6}O_{6.21}$ PD ₂	Ta _{1.25} Pb _{0.75} O _{6.5}	
(Pb-O(1	l))×2	2.330(1	.)	2.329	(6)	2.330(9)	
(Pb-O(2	2))×6	2.738(8	5)	2.709	(11)	2.711(9)	
(<i>M</i> /Pb-	$O(2)) \times 6$	2.035(4	+)	2.048	(6)	2.046(8)	
M = Nb or Ta							

Note. U_{iso} is the isotropic thermal parameter.

g to minimize the difference between calculated and experimental normalized intensity values. SIMPLEX, a multidimensional algorithm is used for minimization. Tables 4a-4c and 5a-5c list the values of the microstructural parameters N, g, and hence D (in Å) along with their standard deviations obtained for the X-ray reflections of 1, 2, 3, and the parent phases. The estimated enthalpy α^* (= $N^{1/2}g$), which physically implies that the growth of the crystals in a particular material is controlled appreciably by the value of g in the net plane structure (20, 21). The corrected experimental X-ray profile that was used for Rietveld analysis was matched with the simulated profile before computing the microstructural parameters as described earlier. A better perspective is to project the crystal size values obtained in terms of (hkl) planes on to a two-dimensional plot, with the D_{hkl} value plotted along the X-axis. It is found that the 222 plane is common in all these phases, which helps in projecting the crystal size on a two-dimensional plane. Further if D_{222} is considered to be the major axis plotted



FIG. 4. MO_6 (M = Nb or Ta) octahedra viewed down the c axis.

along the X direction of an ellipse then the minor axis can be determined by an iterative procedure based on the expression

$$(2D_{hkl}^2) = (\cos \varphi/Y)^2 + (\sin \varphi/X)^2,$$

where φ is the angle between the *hkl* planes. The best value of Y obtained based on the iterative procedure is plotted along the minor axis and denoted as Y_{\min} (Tables 4a-4c, 5a

TABLE 4

hkl	Ν	g (%)	D (nm)	α*
	(a) Microcrystalline	e parameters	of Pb _{1.5} (Ta ₂)O	$7 - \delta$
111	34.4(3)	4.4(1)	21.01	0.257
222	31.3(2)	1.7(1)	9.57	0.096
444	31.3(5)	0.9(1)	4.79	0.048
400	100.2(13)	3.9(1)	26.55	0.395
800	145.7(2.6)	2.1(1)	19.29	0.256
662	145.9(3)	2.3(1)	17.74	0.274
440	152.4(2.8)	3.3(1)	28.55	0.412
622	168.1(1.2)	2.2(1)	28.86	0.281

 $\alpha_{\text{avg}}^* = 0.0.328$; X = 9.57 nm, $Y_{\text{min}} = 8.85$ nm, $Y_{\text{min}}/X = 0.924$; std = 2.8%; $D_{100} = D_{010} = D_{001} = 18.62$ nm; volume (nm³) = 6458.

(b) Microcr	ystalline paran	neters of (2)	
50.4(1)	5.3(1)	15.63	0.377
50.1(8)	3.9(1)	7.79	0.281
46.9(5)	5.3(1)	12.63	0.363
41.2(5)	4.5(1)	5.55	0.291
201.0(8)	1.8(1)	24.82	0.249
46.5(6)	5.5(1)	8.86	0.372
59.1(7)	3.8(1)	9.61	0.291
	(b) Microcr 50.4(1) 50.1(8) 46.9(5) 41.2(5) 201.0(8) 46.5(6) 59.1(7)		(b) Microcrystalline parameters of (2) 50.4(1) 5.3(1) 15.63 50.1(8) 3.9(1) 7.79 46.9(5) 5.3(1) 12.63 41.2(5) 4.5(1) 5.55 201.0(8) 1.8(1) 24.82 46.5(6) 5.5(1) 8.86 59.1(7) 3.8(1) 9.61

 $\alpha_{\text{avg}}^* = 0.252; \ X = 15.63 \text{ nm}, \ Y_{\text{min}} = 4.72 \text{ nm}, \ Y_{\text{min}}/X = 0.302; \ \text{std} = 2.7\%; \ D_{100} = D_{010} = D_{001} = 15.04 \text{ nm}; \ \text{volume} \ (\text{nm}^3) = 3399.$

(c) Microcrystalline parameters of (3)						
222	59.4(3)	4.4(1)	18.49	0.342		
444	66.1(9)	2.7(1)	10.3	0.219		
400	58.8(6)	4.9(1)	15.9	0.372		
800	64.8(12)	2.2(1)	8.73	0.178		
662	89.5(3)	2.3(1)	11.07	0.219		
440	68.2(5)	4.5(1)	13.02	0.368		
622	69.7(5)	2.9(1)	11.34	0.241		
$\alpha_{\text{avg}}^* = 0.274;$ $X = 18.49 \text{ nm},$ $Y_{\text{min}} = 4.96 \text{ nm},$ $Y_{\text{min}}/X = 0.268;$						
std = 1.6%; $D_{100} = D_{010} = D_{001} = 16.06$ nm; volume (nm ³) = 4145.9.						

and 5b; Figs. 6 and 7). The Ta phases show that the crystallite size and volume decrease in the order $2 > 3 > Pb_{1.5}$ (Ta₂)O_{7- δ} (Fig. 6), which explains that reason for broaden-



FIG. 5. Comparison of the X-ray peak widths for samples (2) and (3).



FIG. 6. Comparison of the crystallite shape for (a) $Pb_{1.5}Ta_2O_{7-\delta}$, (b) (2), (c) (3).

hkl	Ν	g (%)	<i>D</i> (nm)	α*
	(a) Microcrystalline	e parameters	of Pb _{1.5} (Nb ₂)O	$7-\delta$
111	60.8(8)	4.6(1)	37.09	0.257
222	60.0(6)	2.1(1)	18.41	0.096
444	60.3(9)	1.4(1)	9.25	0.048
400	159.8(56)	3.4(1)	42.45	0.395
800	150.1(2)	1.1(1)	19.93	0.256
331	150.1(62)	3.1(1)	36.59	0.376
662	150.0(1.5)	1.1(1)	18.27	0.124
440	225.6(6.8)	2.9(1)	42.27	0.431
511	203.6(43)	2.7(1)	41.62	0.385
311	120.3(35)	3.7(1)	38.57	0.405
622	120.3(25)	1.6(1)	19.27	0.175

TABLE 5

 $\alpha_{\text{avg}}^* = 0.279; X = 18.41 \text{ nm}, Y_{\text{min}} = 13.65 \text{ nm}, Y_{\text{min}}/X = 0.744; \text{std} = 3.5\%;$ $D_{100} = D_{010} = D_{001} = 32.63 \text{ nm}; \text{ volume (nm}^3) = 34153.$

	(b) Microcry	stalline paran	neters of (1)	
222	139.4(35)	3.6(1)	43.51	0.428
444	200.8(9)	1.4(1)	31.3	0.201
400	159.8(56)	3.4(1)	43.23	0.425
800	159.0(2)	1.1(1)	21.47	0.139
311	119.9(23)	3.7(1)	75.18	0.408
662	147.9(3.3)	1.6(1)	24.11	0.199
331	150.1(6.2)	3.0(1)	37.23	0.369
662	200.9(26)	1.3(1)	24.87	0.174
440	225.6(68)	2.9(1)	43.09	0.405
$\alpha^{*}_{avg} = 0.308$	$X = 43.51 \text{ nm}, Y_{\text{m}}$	_{in} = 15.94 nm	$Y_{\rm min}/X = 0.36$	56; std = 5.8% ;
$D_{100} = D_{010}$	$D_0 = D_{001} = 49.03$ m	m; volume (ni	$m^3) = 117852.$	

ing of lines in 2 compared to the other two compositions. The trend that is observed in the Nb compositions though is seen to be (Fig. 7) different; i.e., there is a considerable increase in volume and crystallite size in 1 compared to the



FIG. 7. Comparison of the crystallite shape for (a) $Pb_{1.5}Nb_2O_{7-\delta}$ and (b) (1).

Pb-deficient parent phase. Also the average value of α is minimum for the parent phases, indicating phase stabilization in these samples compared to the compositions 1, 2, and 3.

IV. CONCLUSIONS

The Rietveld refinements clearly establish that in substituted lead pyrochlore of the type $Pb_2(M_{2-y}Pb_y)O_{7-\delta}$ (0 < y < 0.8; M = Nb or Ta) the excess Pb is present at the B site. The broadening of the X-ray peaks in 1, 2, and 3 compared to the parent phases causes strain in the lattice due to the addition of Pb in the B site. Strain analysis supports this observation. Compositions 1, 2, and 3 are less stabilized than the parent phase. The oxidation state of Pb in the B site has been conjectured to be 4+ based on comparative studies.

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